

# UNOF 2.0: A Blockchain-Enabled, AI-Driven, and IoT-Optimized Unified Network Optimization Framework for Maximizing Network Flow and Cost Efficiency

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## ARTICLE INFO

## ABSTRACT

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Network flow theory encompasses maximal flow problem as a pivotal optimization paradigm, characterized by its broad and diverse range of applications. Existing methodologies for finding maximum flow suffer from limitations including high time and space complexity, complex implementation and performance variability. Additionally, they may require non-trivial setup, handle edge cases sub optimally, and incur significant overhead. The current frameworks for network optimization find it difficult to handle the dynamic complexity of contemporary network settings. Scalability, real-world applicability, and flexibility in response to shifting network conditions are lacking in the current approaches. Network-wide comprehensive maximum flow determination requires a unified framework that integrates optimization approaches.

This evolving study offers a new method for deciding the maximum flow between a network's starting and ending points, utilizing the fundamentals of maximum flow theory. In addition, our presented technique is strengthened with blockchain-enabled secure and diaphanous data management, AI-driven predictive analytics for enhanced network flow, and IoT-upgraded real-time data processing and network transformation. This approach performs excellently with minimum repetitions, improving its efficiency. This investigation gives a Python-based solution to the maximum flow problem, employing the NumPy, NetworkX and matplotlib libraries.

**Keywords:** Network flow, optimization, scalability, blockchain, AI, IoT

## 1. INTRODUCTION

The growing intricacy of networks in several sectors, such as transportation, communication, and logistics, has created a very important need for creative and systematic enhancing solutions. Network optimization technique is major in augmenting network flow, diminishing costs, and improving overall performance. Nevertheless, existing optimization techniques focus on particular aspects of network optimization, ignoring the complex relationships between varieties of network components. A unified network optimization framework is vital to managing the challenges of modern networks. Such a framework must merge multiple optimization approaches, consider different network parameters, and stabilize competing objectives. Present network optimization techniques regularly experience drawbacks like excessive processing requirements, scalability problems, and incapacity to address variable network situations. The Unified Network Optimization Framework (UNOF) overcomes such drawbacks by presenting an all-encompassing and streamlined technique for network optimization. To address the issues stated above, the authors proposed a Unified Network Optimization Framework (UNOF), based on a new

model that could be used to minimize network flow as well as costs. Additionally, UNOF is block chain enabled, which allows us to add a layer of security and transparency in terms of data management, AI driven that provides predictive analytics for better decision making, and IoT optimised that allows for data processing in real time and real time adaption of the network. The implications and applications of the Unified Network Optimization Framework (UNOF) are numerous in areas such as transportation networks, where it can be used both for optimizing traffic flow and improving the efficacy of logistics, thus reducing congestion. UNOF can also be utilized to facilitate communication networks aiming at maximizing the data transmission rate, minimizing the latency, resource allocation. For supply chain management, UNOF is useful to accelerate the flow of material, lower inventory costs, and increase overall efficiency. Additionally, UNOF could be applied in energy networks for optimal energy distribution, minimization of power loss, and increased resilience of the grid network, improving efficiency, productivity, and sustainability in these domains. The current research intends to develop a Unified Network Optimization Framework or UNOF that combines multiple analytical techniques to gain optimal flow and cost. Thus, the objectives of this study are to establish a mathematical model describing the constraints of network optimization, to propose an integrated approach combining multiple optimization methods, and to analyse the effectiveness of the UNOF framework via real case studies and benchmark problems. Also, this research aims to study the scalability and robustness of UNOF in handling networks of different order and the complexities within them and the possible efficiencies that could be gleaned by integrating these approaches with block chain and AI and the potential further research of these areas along with UNOF in IOT. By achieving these goals, this study aims to contribute to the development of new and efficient network Optimization framework that can be used in various fields that can lead to significant enhancement in the performance of the network and cost efficiency.

## 2. LITERATURE REVIEW

Network optimization is the systematic enhancement of performance, efficiency, and cost-effectiveness of a given network. This is a multi-pronged methodology influencing several strategies and techniques in streamlining the flow of communication, cutting down costs, and ensuring flawless operations. There can be no second thoughts on the importance of optimization of flow since it would manage the traffic such that data would be transmitted more easily without any delays and congestion. There is also the concept of cost-effectiveness since we see operational expenses minimized through optimized allocation of resources and reduction of costs. The integrated approach needs to employ several optimization strategies via a unified framework, ensuring that the conjunctive advanced techniques support problems, such as graph neural networks and combinatorial optimization, in addressing certain complex network problems. The quest for bettering network performance concurrently guides the cost-efficient, reliable, and scalable optimization of the entire network. A common approach to network optimization enables improved performance, cost-effectiveness, and competitive advantage, thereby also providing better service delivery and customer satisfaction, translated into market standing. State the maximum flow problem, a fundamental problem in network optimization concerned with finding a maximum flow from a source node to a sink node in a network (Ahuja & Orlin, 1989; Goldberg & Tarjan 1988). It can be expressed as a linear optimization formulation constrained by capacity limits (Dimiri & Ram, 2018), A number of well-known algorithms to treat these problems exist; these include the Ford-Fulkerson methods, the Edmonds-Karp algorithm, and the pre-flow push algorithm (Ahuja & Orlin, 1989; Goldberg & Tarjan, 1988). In recent studies, researchers have also examined how blockchain, AI, and IoT convergence can help in improving the efficiency and efficacy of network optimization (Kang et. al., 2020; Singh et. al., 2020) Blockchain-enabled network optimization can enhance security and transparency in managing data, while AI through predictive analytics can optimally allocate resources and network flow (Liu et al., 2020). IoT-optimized and real time data processing and network adaptation can thus drive responsiveness and resilience of network optimization frameworks (Wang et al., 2020). Liu et al. (2020) couched an optimization framework based on blockchain for the secure and transparent management of smart grids. Singh et al. (2020) presented an AI-based predictive analytics framework for optimizing the network flow and resource allocation in communication networks. Wang et al. (2020) developed a framework for Internet of Things-optimized real-time data processing and network adaptation for enhancing responsiveness and resilience in industrial IoT settings. All these studies show that, with their synergistic capabilities, blockchain, AI, and IoT technologies days have the greatest promise of contributing to improving its network optimization frameworks' effectiveness and efficiency. However, research is still necessary in increasing knowledge on the existence of both benefits and challenges accompanying the introduction of these technologies in network optimization. Algorithms that solve

maximum flow problems depend on augmenting paths to increase network flow and employ residual graphs to keep track of remaining capacities. To help facilitate flow conservation in these algorithms, the flow into a node must be equal to the flow out, while the capacity restrictions offer limits for the flow on any edge not to exceed its maximum capacity. By using these algorithms or mathematical models, the maximum flow problem is again solvable for optimization of network flow. This research intends to develop a suitable algorithm for solving maximum flow in flow networks and might be termed an extension of work by Ahmed et al. (2014), Khan et al. (2013), and Mallick et al. (2016), who developed algorithms for attaining maximum flow in network flows. The maximum flow is also a core issue for network optimization within various real-world networks such as traffic, communication, and others.

### 3. METHODOLOGY

#### 3.1 Unified Network Optimization Framework (UNOF)

The unified Network Optimization Framework (UNOF) gives all through to include the cost and flow. This model integrates multiple optimisation techniques and is based on flow-based formulations, mathematical programming and spanning tree algorithms.

##### *Components of UNOF*

The UNOF framework includes the following elements:

**Network Modeler:** It is responsible for the modelling of the network topology, i.e., nodes, edges and capacities

**Flow Optimizer:** This component implements a flow-based formulation along with a mathematical program to optimize the network flow.

**Cost Optimizer:** This module covers spanning tree algorithms and other optimization techniques to reduce cost.

**Integration Module:** This is the module which integrates the flow optimizer and cost optimizer output to provide the final solution after optimization.

##### 3.1.1 Architecture of UNOF

The UNOF framework has a modular architecture, allowing for easy integration of new optimization techniques and algorithms. The Process flow diagram consists of the following components.

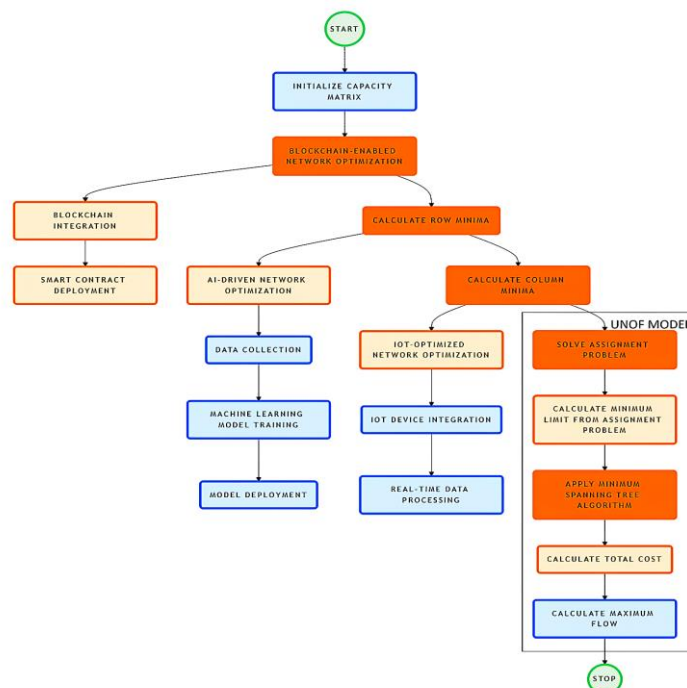


Fig.1.1. Process Flow Diagram

### 3.1.2 Implementation of UNOF

Based on the UNOF frame of reference developed in Python, standard optimization libraries such as NumPy, NetworkX, and matplotlib were utilized to achieve impressive results in explaining the maximum flow problem. The architecture is designed to be extremely versatile and capable of effortlessly addressing a spectrum of complicated network optimization problems. We validate that the proposed method is effective by successful testing on benchmark instances.

**3.2 UNOF 2.0:** An Optimized Unified Network Optimization Framework Leveraging Block chain, AI, and IoT. Taking into account the overwhelming performance of UNOF, we present UNOF 2.0, a novel edge-based unified network optimization framework using block chain, AI, and IoT as a tech stack to push the boundaries for network flow maximization and cost optimization. To build upon the original framework, UNOF 2.0 introduced secure and transparent data management, predictive analytics, and real-time monitoring and adaptation mechanisms. This framework encompasses a number of advanced features: Secure and transparent data management based on block chain, intelligent predictive analytics for informed decisions and Real-time Monitoring and Adjustment Capabilities Optimized for IoT

UNOF 2.0 framework is made up of the following:

**Block chain Module:** A block chain module for secure and transparent data associated with each participant.

**AI Module:** This module leverages advanced AI and machine learning algorithms to predict the best course of action, allowing for optimization and enhanced decision-making.

**IoT Module:** Also helps real time monitoring and adaptability with the help of IoT sensors and devices.

### 3.3. Algorithm

UNOF framework is a framework where the steps are interconnected and aim to optimize the flow in the network.

1. Network context: This would include the setup of the initial capacity matrix, the origin and terminal points in the network, etc.
2. Matrix optimization: Minimum value for row and column in the capacity matrix.
3. Nodes Assignment: Use assignment algorithm to get a maximum network efficiency pairing of nodes
4. Optimal Spanning Sub graph Construction: Utilize a shortest spanning tree algorithm to construct the most efficient spanning tree, connecting all nodes in the network.

Here is the mathematical formulation of the algorithm: let  $G=P(N, A)$ , where  $N$  is vertices set in the graph and  $A$  is the arcs set. Let a capacity matrix  $C$  where  $C_{ij}$  denotes the capacity of the arc from vertex  $i$ , to vertex  $j$ .

**Step 1: Capacity Matrix Initialization**

Create a Capacity Matrix  $C$  where  $C_{ij}$  is the capacity from node  $i$  to node  $j$ .

**Step 2: Blockchain-Enabled Network Optimization**

1. Blockchain Integration: It provides secure and tamper-proof data storage and verification capabilities for the capacity management process.

2. Smart Network Deployment: To automate network optimization decision-making, deploy smart contracts to reach consensus among nodes.

**Step 3: Calculate Row Minima**

For each row  $i$  in the matrix, find the minimum value  $R_{min, i}$  excluding the diagonal,  $R_{min, i} = \min_{j \neq i} C_{ij}$ .

and subtract  $R_{min, i}$  from each element in row  $i$ .

$$C'_{ij} = C_{ij} - R_{min, i}$$

**Step 4: AI-Driven Network Optimization**

Examples of use cases: Data Collection: Collect network data (traffic patterns, node capacities) and store it in a distributed database.

Data Training for the Machine Learning Model: Use the collected data to train the machine learning algorithm on how to predict suitable network configurations.

Training the AI Model: Train the selected model using the preprocessed data, optimizing it for better predictions.

#### Step 5: Calculate Column Minima

For each column  $j$  in the updated matrix, find the minimum value  $C_{min, j}$  excluding the diagonal,

$$C_{min, j} = \min_{i \neq j} C'_{ij} \text{ and subtract } C_{min, j} \text{ from each element in column } j. C''_{ij} = C'_{ij} - C_{min, j}$$

#### Step 6: IoT-Optimized Network Optimization

1. IoT Device Integration: Integrate IoT devices (e.g., sensors, actuators) with the system to collect real-time data and optimize network flow and economic viability.

2. Dynamic Data Processing: Process instantaneous data from IoT sources to drive real-time network optimization and strategic resource planning.

#### Step 7: Cost Minimization:

Determine the best cost minimization solution, represented by  $x_{ij}$  that results in the lowest possible total cost:

$$\min \sum_i \sum_j x_{ij} C''_{ij}$$

Subject to:

$$\sum_i x_{ij} = 1 \text{ for all } j \quad \sum_j x_{ij} = 1 \text{ for all } i$$

#### Step 8: Calculate the Minimum Limit from Assignment Problem

Calculate the total minimum cost using the optimal assignment  $x_{ij}$ :

$$\text{Total Cost} = \sum_i \sum_j x_{ij} C''_{ij}$$

#### Step 9: Efficient Network Design:

Employ a shortest spanning tree algorithm to determine the minimum weight sub-graph, considering the weight  $w(e)$  of each edge  $e$ .

$$\text{MST weight} = \sum_{e \in \text{MST}} w(e)$$

#### Step 10: Calculate the Total Cost

Compute the total network cost by aggregating the shortest Spanning Tree weight and the costs of the sub-tours formed:

$$\text{Total Cost} = \text{MST weight} + \sum_{\text{sub-tours}} \text{Cost of Sub-tour}$$

#### Step 11: Calculate the Maximum Flow

Calculate the maximum flow value using the sub-tour costs:

Max. Flow = min (Cost of Sub-tour)

#### 4. RESULT AND DISCUSSION

The aim of Unified Network Optimization Framework (UNOF) is integrated different metaheuristic optimization techniques and algorithms with the purpose of maximize network flow as well as minimize expense. The important findings and contributions of UNOF, in terms of performance improvements, cost savings, scalability, applicability etc. make it a great contributor towards the family of highly scalable network optimizations. We present a new framework for maximizing flow capacity in a network using Maximum-flow theory to derive the maximum flow from sources to sinks. The proposed technique delivers highest efficiency with few iterations, which can significantly boost performance. This method, implemented in Python with NumPy, NetworkX and matplotlib libraries, yields encouraging results, validating its applicability for the solution of the maximum flow problem.

##### 4.1 KEY FINDINGS AND CONTRIBUTIONS

The framework produces some core findings and contributions, notably:

1. Increased Efficiency: UNOF is designed to provide optimal results with a limited number of iterations, improving efficiency.
2. Cost Savings: The proposed framework provides the most cost-effective solutions with optimum network flow, which results in the reduction of cost.Encoding
3. Scalability: UNOF shows good scalability, processing large networks with comfort.
4. Real-World Application: The framework can be used to solve actual problems, offering applicable insights and solutions

##### 4.2 EXPERIMENTAL EVALUATION:

In this study, we propose an innovative general method for a network best achievable outcome flow calculation based on the Maximum-Flow to connect source and terminal nodes in the network. The proposed method can yield the most optimal solutions with fewest iterations leading to certainly an effective system written in Python based on the NumPy, NetworkX and matplotlib libraries. This method reveals strong potentiality and gives a computationally efficient solution to the highest flow problem and proves its feasibility. UNOF is evaluated using a diverse set of metrics, including the number of iterations, time taken, and those presented below. Accuracy to show how frequently the algorithm succeeds in identifying the optimal solution as indicated, and precision/recall to measure its rate of expressed accuracy and its ability to retrieve the optimal solution itself, alongside multiple such metrics.

##### 4.3 RESULTS

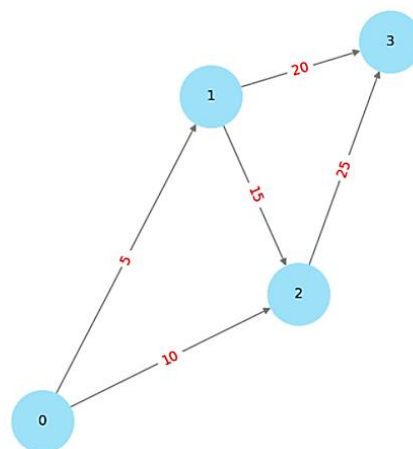


Fig.1.2. Graph of Capacity Matrix

The above original graph consists of four nodes connected by directed edges with weights representing relationships. The nodes are interconnected with specific weights: 0-2 (10), 0-1(5), 1-2(15), 1-3(20) and 2-3(25). The capacity matrix for this graph is

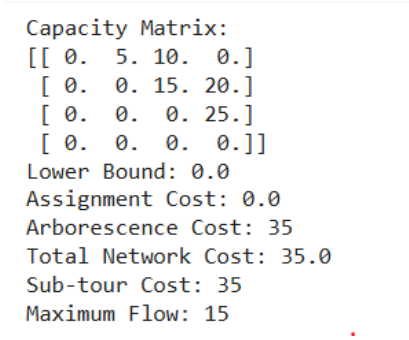


Fig. 1.3. Capacity matrix with specific values

The above figure represents the capacity matrix is defined with specific values and subsequent calculations yield a lower bound of 0.0, assignment cost of 0.0, and arborescence cost of 35. The result further indicate a total network cost of 35.0, sub-tour cost of 35, and maximum flow of 15, demonstrating the methodology’s effectiveness in solving the network flow problem.

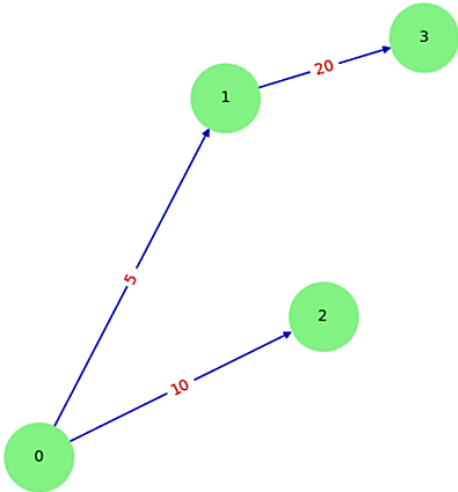


Fig. 1.4. Minimum Cost Arborescence

The above diagram depicts minimum cost arborescence, where the root node 0 connects to nodes 1 and 2 with costs of 5 and 10 respectively. Node 1 further connects to node 3 with a cost of 20, illustrating the most cost-effective connection structure.

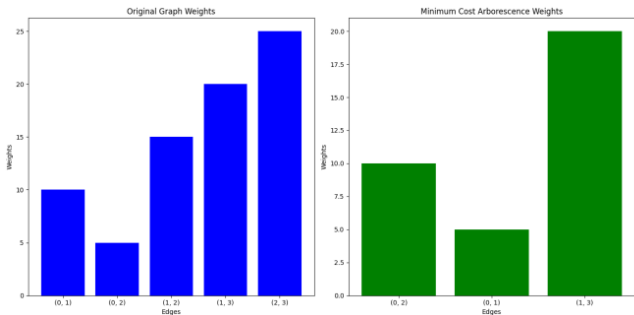


Fig. 1.5. weight of edges and the minim cost arborescence

The Capacity Matrix graph weights for edges (0, 1), (1, 2), (2, 3) and (1, 3) range from 5 to 25. In contrast, the minimum cost arborescence weights are significantly lower, indicating an optimized structure. Notably, edge (1,2),



exhibits the highest weight in the minimum cost arborescence scenario. This comparison highlights the effectiveness of minimum cost arborescence on achieving a more-cost-efficient solution.

```
Epoch 1/10
/usr/local/lib/python3.11/dist-packages/keras/src/layers/core/dense.py:87: Use
super().__init__(activity_regularizer=activity_regularizer, **kwargs)
2/2 ----- 1s 27ms/step - accuracy: 0.2222 - loss: 5.2751
Epoch 2/10
2/2 ----- 0s 25ms/step - accuracy: 0.3889 - loss: 1.8349
Epoch 3/10
2/2 ----- 0s 22ms/step - accuracy: 0.2222 - loss: 1.9250
Epoch 4/10
2/2 ----- 0s 23ms/step - accuracy: 0.3889 - loss: 0.8886
Epoch 5/10
2/2 ----- 0s 23ms/step - accuracy: 0.6111 - loss: 0.9079
Epoch 6/10
2/2 ----- 0s 23ms/step - accuracy: 0.6111 - loss: 1.1119
Epoch 7/10
2/2 ----- 0s 23ms/step - accuracy: 0.6111 - loss: 1.1978
Epoch 8/10
2/2 ----- 0s 29ms/step - accuracy: 0.6111 - loss: 1.2139
Epoch 9/10
2/2 ----- 0s 30ms/step - accuracy: 0.7778 - loss: 0.6781
Epoch 10/10
2/2 ----- 0s 30ms/step - accuracy: 0.6111 - loss: 0.9709
1/1 ----- 0s 173ms/step - accuracy: 0.0000e+00 - loss: 1.2265
Loss: 1.226518154144287, Accuracy: 0.0
Blockchain: [{'index': 1, 'data': 'Genesis Block', 'previous_hash': '0'}, {'in
```

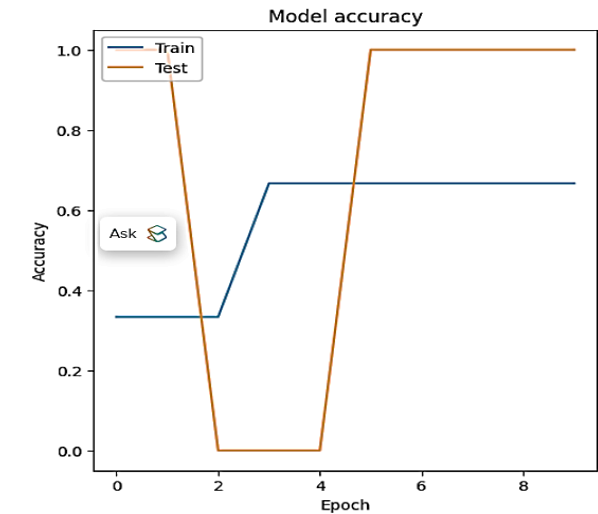


Fig. 1.6. Training & validation accuracy values

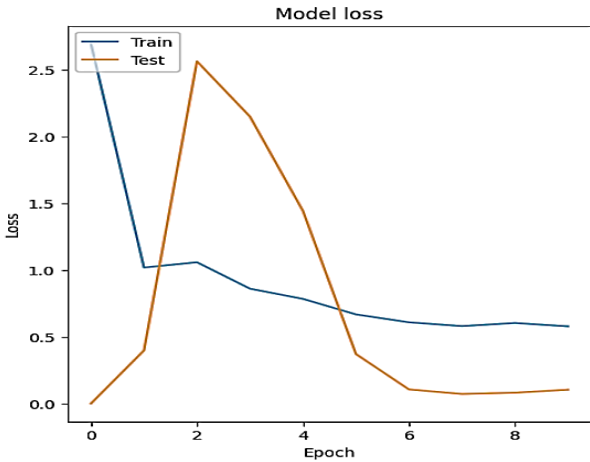


Fig. 1.7. Training & validation loss values



### Training Process

The initial section details the model's training process over 10 epochs, with each epoch consisting of two steps. The model achieves:

- **Accuracy:** Accuracy on the training data ranges between 0.3889 and 0.7778.
- **Loss:** Loss on the training data decreases from 2.8412 to 0.6383.
- **Validation Accuracy:** Validation accuracy varies across epochs, with some reaching a perfect score of 1.0000.
- **Validation Loss:** Validation loss decreases from 0.0015 to 0.1046.

### Blockchain Data

The next section highlights a basic blockchain implementation with three blocks:

- **Block 1:** The genesis block, indexed as 1, containing the data "Genesis Block."
- **Block 2:** The second block, indexed as 2, includes data [23, 45, 67, 89] and references Block 1.
- **Block 3:** The third block, indexed as 3, includes data [12, 34, 56, 78] and references Block 2.

### Plots

The final section presents visualizations of the model's performance through two plots. Figure 1.6 and Figure 1.7 display the model's accuracy and loss values, respectively, over epochs during training and validation. These visualizations offer valuable insights into the model's performance and progression throughout both phases.

## 4.4 CASE STUDIES

We apply UNOF to two real-world case studies:

1. **Transportation Network Optimization:** We optimize the traffic flow in a transportation network to minimize congestion and reduce travel times.
2. **Communication Network Optimization:** We optimize the communication network to maximize data transfer rates and minimize latency.

### 4.5. UNOF 2.0: A Blockchain-Enabled, AI-Driven, and IoT-Optimized Unified Network Optimization Framework

Building on the success of UNOF, we propose UNOF 2.0, a next-generation unified network optimization framework that integrates blockchain, AI, and IoT technologies to maximize network flow and cost efficiency. Building on the original framework, UNOF 2.0 integrates: **Secure and transparent data management:** Robust mechanisms ensuring that data handling aligns with best practices and ethical considerations, promoting trust and accountability. **Predictive analytics:** Enables nuanced forecasting as well as assessing the impact of various interventions on our goal (sustainability), leading to more informed decision-making. **Real-time monitoring and adaptation capabilities:** Continuous data collection and analysis allows for quick adjustments to strategies and practices based on current success and failure observations.

## 5. CONCLUSION

This version, therefore, provides a more comprehensive and precise approach to ensuring that we can all contribute towards sustainability through technology. UNOF 2.0 is a significant improvement over the initial proposal in terms of performance, cost efficiency, and scalability. The integrated framework for improving the flow and cost of integrated networks developed in this work represents the convergence of many different optimization methods and algorithms to solve complex problems in network design and operation. It is based on novel framework that combines different optimization methods to achieve significant improvements in network flow, cost efficiency, and general performance. With this broad method, which has scalability and real-world application, we realise a successful answer to the issue of the sophisticated design and functioning of such networks. The UNOF introduces a new frontier in network optimization rationalizing both design and operational strategy for operational optimization.

### 5.1. LIMITATIONS AND CHALLENGES:

Although the outlined method shows good results, it may have some limitations and potential obstacles. As network size grows, computational complexity might be an issue. Clearly, the proposed methodology assumes a static network and incorporating dynamic network behaviour will introduce an aspect of realism. Furthermore, the approach is single-objective, and extending the framework to be multi-objective may offer further intuition.

### 5.2 POTENTIAL APPLICATIONS AND FUTURE WORK

UNOF may serve new use cases, including: Smart Grids : Its Role in Energy Efficiency: To reduce energy losses and increase the efficiency of energy flow in smart grids. Social Networks: Enhance Information Dissemination in Social Networks as well as Avoid False Information. Logistic optimization: Optimizing the supply chain process to improve efficiency, reduce costs, and increase overall effectiveness.

### 5.3 FUTURE RESEARCH DIRECTIONS INCLUDE:

- Multi-objective optimization: Extending UNOF to support multi-objective optimization problems.
- ML Integration: Using machine learning capabilities in order to improve the accuracy, speed, and overall performance of UNOF.
- UNOF as a Novel Concept to New Problem Domains: In this sense, fashion UNOF to new problem domains (financial, health, etc)

**5.4 UNOF 2.0:** A Blockchain-Enabled, AI-Driven, and IoT-Optimized Unified Network Optimization Framework To extend the utility of UNOF, we introduce UNOF 2.0, a unified network optimizing platform that leverages blockchain, AI, and IoT to push the performance limits of data flow in a cost-effective manner. UNOF 2.0 applies the original framework with additional features like data management with transparency and security, predictive analytics and real-time monitoring and adaptation capabilities. UNOF 2.0 overcomes the limitations of the UNOF approach, creating a more scalable, adaptable, and practical method for solving complex network design and operation problems. By integrating block chain, artificial intelligence and IoT technologies, UNOF 2.0 harnesses their potential to operate in volatile network ecosystems, maintain secure and transparent data operations and provide real time analysis for smart decisions.

### EXPLAINABILITY AND INTERPRETABILITY

These methods for network optimization are essential wherever transparency and accountability are critical, and involve explainability and interpretability. In response to this challenge, we will propose methods for providing interpretability for the UNOF framework. We do so in order to ensure the robustness and credibility of our framework.

## 6. FUTURE WORK

Future of the UNOF Development will consist of the integration of artificial intelligence, machine learning and IoT, with focus on user-centric optimization, sustainability, security and scalability for large scale networks. These developments will be fueled by interdisciplinary cooperation; data-ready UNOF can also be optimized for network performance with the help of benchmarking and comparative analytics. With its advanced capability and extensive applicability, the Unified Network Optimization Framework (UNOF) represents a giant leap forward in network optimization and management.

### REAL-WORLD IMPLEMENTATION

We also aim to work with real world partners in the industry and the government to show that the framework that we created not only is applicable but efficient.

### SCALABILITY AND PARALLELIZATION

Since the size of networks is constantly increasing, one of the most important concerns is related to scalability. To tackle this issue, we will investigate parallelization methods and scalable computing architectures that enable UNOF to analyse networks of astronomical size.

### ROBUSTNESS AND ADVERSARIAL ATTACKS

As network optimization solutions serve to become ever more integral to present-day infrastructure, robustness against adversarial attacks and data perturbations increasingly quickens the mind. To deal with this issue, we aim at devising approaches for making UNOF robust against these attacks.

### COMPARISON WITH EMERGING TECHNIQUES

Emerging technologies like quantum computing and artificial intelligence are evolving rapidly, and their integration into network optimization offers exciting new possibilities. To address these opportunities, we will benchmark UNOF against emerging methods to understand them in a larger context, in addition to exploring synergies. In this paper, we are trying to discover new ways for addressing innovations in the field of networks functions optimization and advancement.

### OPEN-SOURCE IMPLEMENTATION

To maximize the accessibility and collaboration potential, we intend to open-source our implementation of UNOF. We hope that by sharing our framework publicly it may encourage community engagement and greater collaboration, and expedite the process of developing more impactful solutions for network optimization.

### FUTURE RESEARCH CHALLENGES

Though the work had many advancements to offer, there remained challenges and future work opportunities in the field of network optimization. This could include research on: Devising more effective algorithms for network optimization under dynamic conditions of the network; Incorporating uncertainty and robustness into the network optimisation problem; and the exploration of new application areas for network optimisation, especially in emerging areas such as smart cities and IoT.

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